# CASCADED INTEGRATOR COMB

SystemC Approach

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## 1 Introduction

Cascaded Integrator Comb (CIC) filter is one of the most popular filters in literature. Its main advantages are a) no multipliers b) implemented as recursive (IIR) or non-recursive (FIR) as well. The attached code is corresponding to the non-recursive implementation which is depicted by (1) and shown in Fig. 1.

Recursive representation

$$H(z) = \left(\frac{1}{\alpha} \frac{1 - z^{-\alpha}}{1 - z^{-1}}\right)^N \tag{1}$$

....

where  $\alpha = M \times D$ , M decimation factor and D differential factor where  $D \in \{1, 2\}$ .

Non-Recursive representation

$$H(z) = \left(\frac{1}{\alpha} \sum_{i=0}^{\alpha-1} z^{-i}\right)^N \tag{2}$$

Non-Recursive representation

$$H(z) = \left(\prod_{i=0}^{\beta-1} (1+z^{-2^{i}})\right)^{N}$$
(3)

where  $\beta = log_2(\alpha)$ .

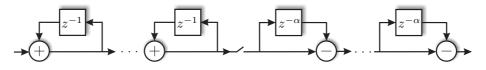


Figure 1: IIR-FIR CIC implementation.

## 2 Getting Stared

The SYSTEMC model for the CIC is developed in structural hierarchal manner. In other words, each component is design individually in a header file. Further, each component has its own source file to test the corresponding block separately from the top-level entity. The top-level entity "cicDecimator.h" combines all the sub-blocks "integrator.h", "comb.h" and "downsample.h" to form a CIC decimation filter. The test-bench is given in "cicDecimator.cpp".

### 3 How to use the code?

You can customize the code to fits your specs. You need to enter/change the decimation factor M and the filter order or the number of stages N. You can do so by replacing M at "downsample.h"

Input	1 <sup>st</sup> Integrator Output	2 <sup>nd</sup> Integrator Output	3 <sup>rd</sup> Integrator Output	1 <sup>st</sup> Comb Output	2 <sup>nd</sup> Comb Output	3 <sup>rd</sup> Comb Output
0	0	0	0	0	0	0
1	1	1	1	1	1	1
1	2	3	4	3	2	1
1	3	6	10	6	3	1
1	4	10	20	10	4	1
1	5	15	35	15	5	1
1	6	21	56	21	6	1
1	7	28	84	28	7	1

Figure 2: 3 stages CIC (N = 3, M = 1) estimated output stage by stage.

Time <sup>CLR</sup>		1		1	100 B		1	1	1	1	-
CLK											
CICIN	0	<u>(1</u>									
I(0)	0	χ1	X2	)(3	<u>X</u> 4	χ5	χ6	χ7	)(8	χ9	χ10
I(1)	0	<u>(1</u>	χз	)(6	χ10	χ15	χ21	χ28	(36	χ45	χ55
I(2)	0	<u>(1</u>	χ4	)(10	χ20	<u>)</u> (35	χ56	χ84	)(120	X165	X220
C(0)	0	χ1	χз	χ6	χιο	<u>χ</u> 15	)(21	χ28	X36	χ45	<u>χ</u> 55
C(1)	0	χ1	χ2	χз	χ <u>4</u>	χ5	χ6	χ7	χ8	χ9	χ10
C(2)	0	χ1									
cicOUT	0	χ1									

Figure 3: CIC simulated (N = 3, M = 1) output stage by stage.

Input	1 <sup>st</sup> Integrator Output	2 <sup>nd</sup> Integrator Output	3 <sup>rd</sup> Integrator Output	M	1 <sup>st</sup> Comb Output	2 <sup>nd</sup> Comb Output	3rd Comb Output
0	0	0	0	0	0	0	0
1	1	1	1	0	0	0	0
1	2	3	4	4	4	4	4
1	3	6	10	4	4	4	4
1	4	10	20	20	16	12	8
1	5	15	35	20	16	12	8
1	6	21	56	56	36	20	8
1	7	28	84	56	36	20	8
1	8	36	120	120	64	28	8

Figure 4: CIC decimator (N = 3, M = 2) estimated output stage by stage.

TTIIG												
CLR												
CLK												
cicIN	0	χ1										
Ι(Ο)	0	)(1	χ2	)(3	χ4	χ5	)(6	χ7	)(8	χ9	)(10	
I(1)	0	)(1	χз	<u>)</u> (6	)(10	χ15	21	)(28	X36	X45	(55	χ66
I(2)	0	)(1	χ4	<u>)(10</u>	)(20	X35	<u>χ</u> 56	)(84	X120	<u>χ</u> 165	)(220	χ28
SlowClock												
HandOff	0			χ4		χ20	נ	(56		)(12	0	
C(0)	0			χ4		χ1.	5	(36		)(64		
C(1)	0			χ4		χ1:	2	(20		)(28		
C(2)	0			χ4		χ8						
CICOUT	0			χ4		χ8						
CICOUT	0			<u>X</u> 4	_	<u></u>						

Figure 5: CIC decimator (N = 3, M = 2) simulated output stage by stage.

#### #define M 2

Then at "**cicDecimator.h**" replace the N

#### #define N 3

Finally, you can change the clock frequency and enter your stimuli at the "cicDecimator.cpp"

sc\_clock CLK("CLK", 10, SC\_NS);

•

. cicIN = 0;